

**OBJECTIVE:** Students will be able to compute permutations and solve problems involving object ordering.

**CHECKPOINT:**

A club with 10 people is electing a president, vice-president, and treasurer. How many different ways can a president, vice-president, and treasurer be selected from among the ten?

**REACH:**

Candice has 5 cards displaying the digits shown:



How many different 3-digit numbers can be created using Candice's cards?



## LAUNCH

- 1 You are the judge at a dog show, and you must award a Gold, Silver, and Bronze ribbon to **THREE** dogs out of the field shown.



How would you award the ribbons?



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- 2 How many different ways can the medals be awarded?

## SKILL REVIEW

**3** Solve:  $\frac{10!}{7!}$

**4** How many different ways can **EIGHT** books be rearranged on a bookshelf?

**5** How many different ways can the letters:

**A, B, C, D, E, F**

be arranged, if you know that the letter **A** must come first?

The word *permutation* means a unique arrangement of things where the order matters. Each permutation is a different arrangement of the objects.

For example, if you have the digits 3, 4, 5, then the arrangements

**345, 354, 453, 435, 543, 534**

are all permutations of these objects. There are **SIX** ways in which these digits can be uniquely arranged, so these are the six permutations of the digits 3, 4, 5.

- 6** How many permutations can be made from the letters in the word **S-K-A-T-E-R**?

**But what if you wanted to select only a small number of objects from a large set?**

- 7** For example, **TEN** gymnasts are competing for **Gold, Silver, and Bronze** medals. How many different ways can these **THREE** medals be awarded?

**In this case, you selecting from a set of TEN, but only creating permutations by arranging THREE of the "objects" at a time. To solve this, we use the notation:**

$${}_{10}P_3$$

**This means: compute 10!, but only use the first THREE factors (10 x 9 x 8).**

## PRACTICE

Compute each factorial.

8  ${}_5P_3$

9  ${}_8P_2$

10  ${}_{12}P_1$

11  ${}_4P_4$

12  ${}_7P_4$

13  ${}_{10}P_3$

14  ${}_8P_5$

15 How many 4-digit passwords can be made selecting from the letters A-B-C-D-E-F-G-H, if each letter can only be used once per password?

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### LOOKING AHEAD

16 A pizzeria offers 5 toppings:

**Pepperoni**

**Olives**

**Mushrooms**

**Tomatoes**

**Ham**

How many different 3-topping pizzas are possible?

(HINT: the answer is NOT 60)

## CONCLUSION

- 17** Copy the formula that goes with *permutation notation*:

Arrange  $r$  items from a set of  $n$  items:

$${}_n P_r = \frac{n!}{(n-r)!}$$

Use the formula, and show all work, to compute:

$${}_9 P_6$$

- 18** Calvin has recorded **EIGHT** songs, and needs to create a demo CD with his best **THREE** songs.

How many unique three-song demo CDs can be made using different combinations of these eight songs?

**Instructional Objectives**

**Standard 18.0.3**

**Students will be able to compute permutations and solve problems involving object ordering.**

Were you 100% focused and engaged during today's lesson?

**Yes**

**No**

**%**

Rate your understanding of the instructional objective.

**4**

completely understand

**3**

mostly understand

**2**

understand a little

**1**

a bit confused

**0**

completely confused

Please take a minute to help me gauge your understanding by answering the following question.

**How many different THREE-digit PINs can be made using only the letters:**

**A-B-C-D-E-F**

**if none can be repeated?**

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